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# Simulations of particle beam heating of foils for studies of warm dense matter\*



J. J. Barnard<sup>1</sup>, A. Friedman<sup>1</sup>, B. G. Logan<sup>2</sup>, M. M. Marinak<sup>1</sup>, R. M. More<sup>2</sup>,  
G. E. Penn<sup>2</sup>, P. Santhanam<sup>2</sup>, J. S. Wurtele<sup>2</sup>, and S. S. Yu<sup>2</sup>

American Physical Society, Division of Plasma Physics Meeting

October 24-28, 2005

Denver, Colorado

1. Lawrence Livermore National Laboratory

2. Lawrence Berkeley National Laboratory

\*Work performed under the auspices of the U.S. Department of Energy under University of California contract W-7405-ENG-48 at LLNL, and University of California contract DE-AC03-76SF00098 at LBNL.

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# Abstract

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We present simulations of particle beam heating of target foils using the multi-physics radiation hydrodynamics code HYDRA<sup>\*\*</sup>. We simulate possible targets for a near-term experiment at LBNL (the so-called Neutralized Drift Compression Experiment, NDCX) and possible later experiments on a proposed facility (NDCX-II) for studies of warm dense matter. Simulation results are presented showing the degree of temperature uniformity and the maximum temperature expected. Various target materials (including aluminum, aluminum foam, water ice, and gas jets) and target configurations are presented. Strategies for characterizing the material equation of state, using data from the experiments together with simulations, will be discussed. Requirements on the NDCX-II accelerator, based on target considerations, will also be discussed.

<sup>\*\*</sup>M. M. Marinak, G. D. Kerbel, N. A. Gentile, O. Jones, D. Munro, S. Pollaine, T. R. Dittrich, and S. W. Haan, Phys. Plasmas 8, 2275 (2001).

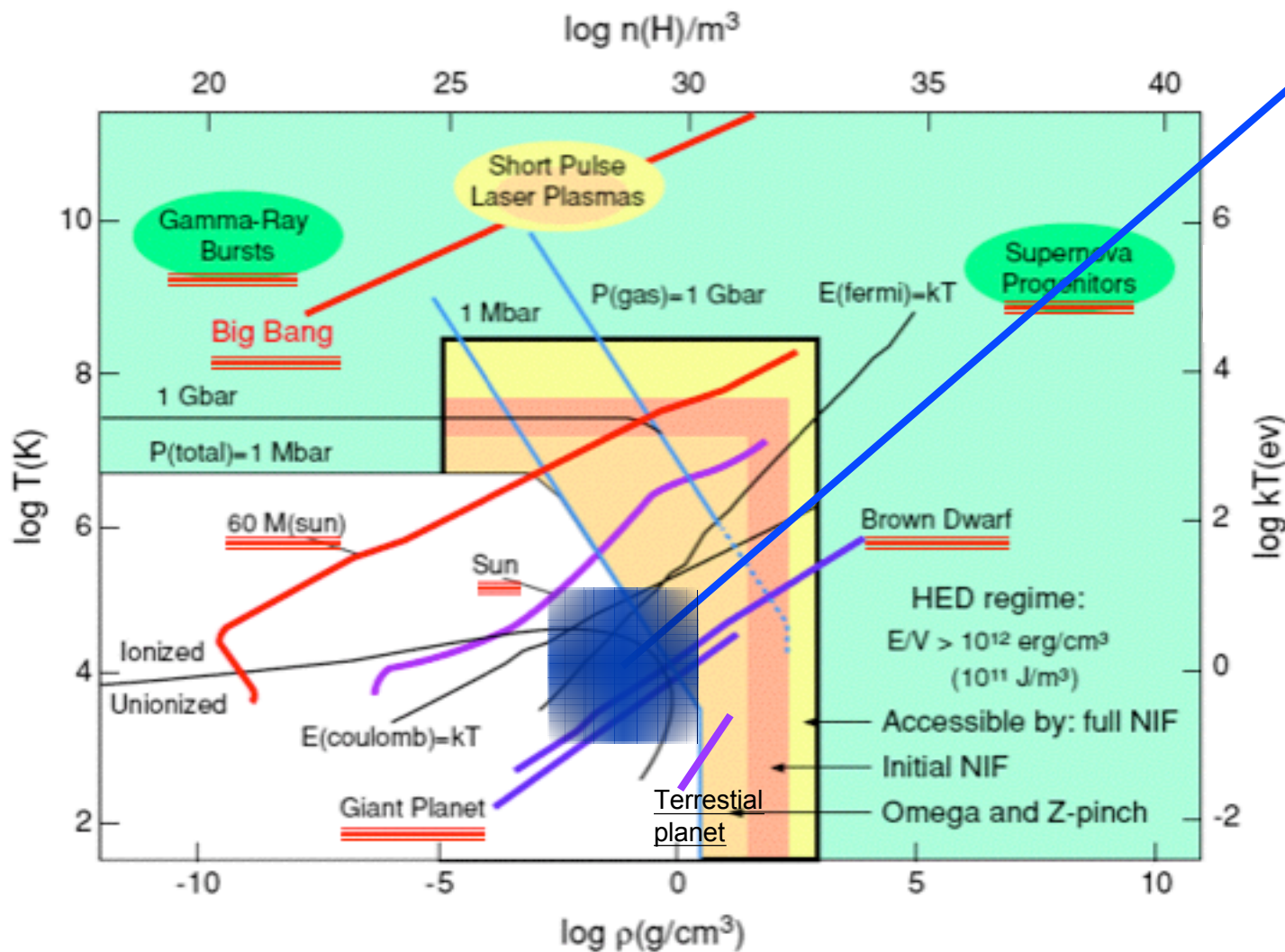
# Outline of poster

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- 1. Motivation for accelerator driven Warm Dense Matter studies**
- 2. Parameters of current and proposed accelerators**
- 3. Simulations of target experiments**
  - Validation of uniformity**
  - Explorations of two-phase regime**
    - Existence of temperature/density “plateaus”**
  - Rayleigh-Taylor instability using ion deposition**
  - Other experiments**

# The $\rho - T$ regime accessible by beam driven experiments lies square in the interiors of gas planets and low mass stars

Figure adapted from “Frontiers in HEDP: the X-Games of Contemporary Science:”



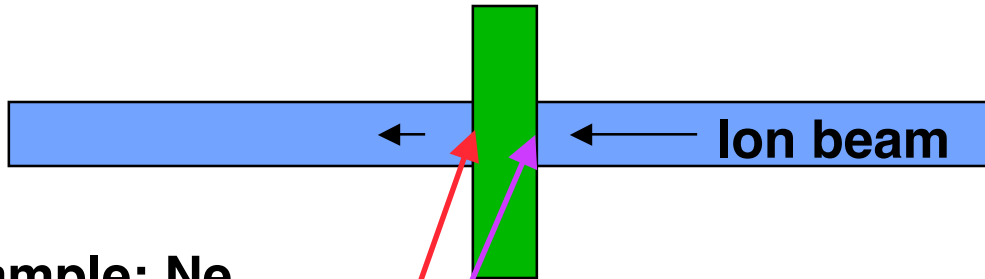
Accessible region using beams in near term

Region is part of Warm Dense Matter (WDM) regime

WDM lies at crossroads of degenerate vs. classical and strongly coupled vs. weakly coupled

# Strategy: maximize uniformity and the efficient use of beam energy by placing center of foil at Bragg peak

In simplest example, target is a foil of solid or “foam” metal



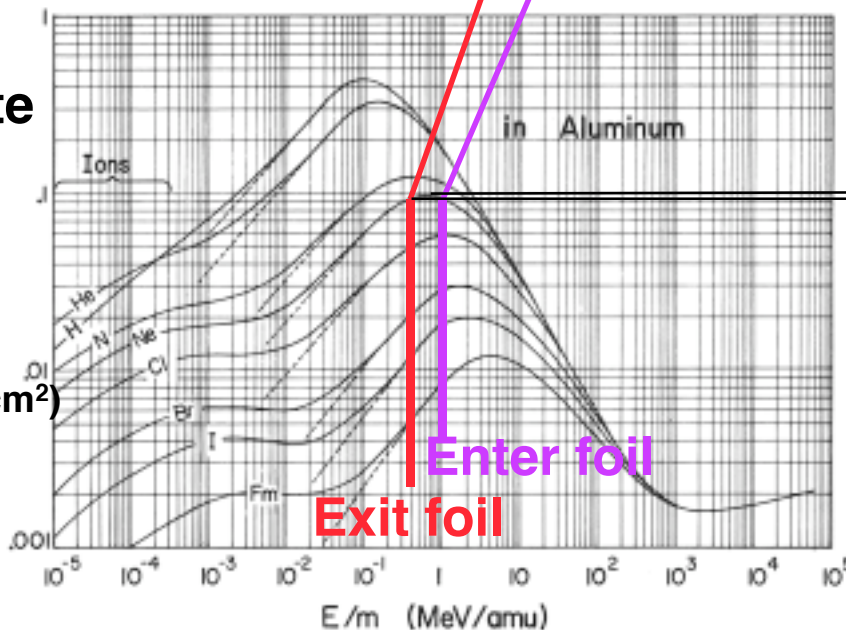
fractional energy loss can be high and uniformity also high if operate at Bragg peak (Larry Grisham, PPPL)

Example: Ne

Energy loss rate

$$-\frac{1}{Z^2} \frac{dE}{dX}$$

(MeV/mg cm<sup>2</sup>)



Energy/ion mass (MeV/amu)

$$\Delta dE/dX \propto \Delta T$$

In example,

$$E_{\text{entrance}} = 1.0 \text{ MeV/amu}$$

$$E_{\text{peak}} = 0.6 \text{ MeV/amu}$$

$$E_{\text{exit}} = 0.4 \text{ MeV/amu}$$

$$(\Delta dE/dX)/(dE/dX) \approx 0.05$$

(dEdX figure from L.C Northcliffe and R.F.Schilling, Nuclear Data Tables, A7, 233 (1970))

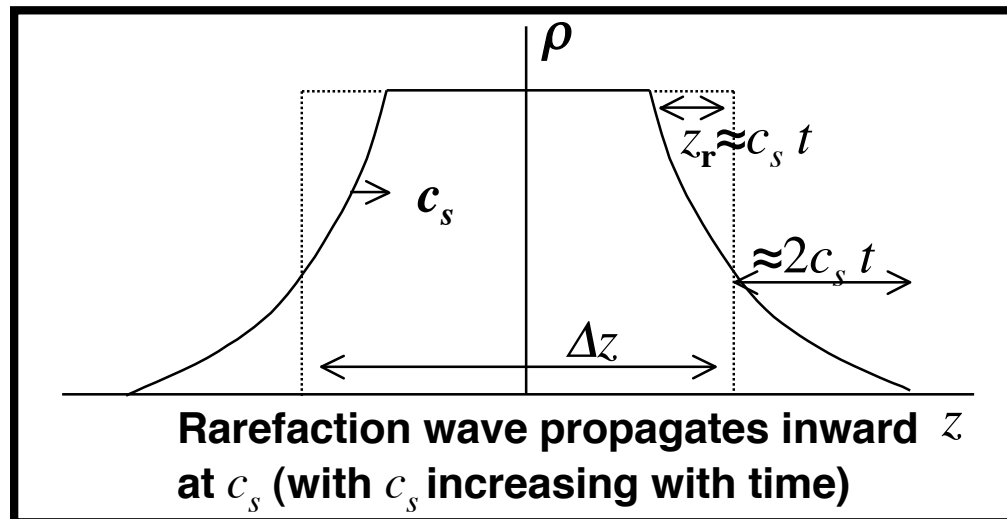
# Pulse duration must be short to avoid hydrodynamic expansion and cooling

$$\tau_{\text{pulse}} < z_r / c_s$$

Here:  $\tau_{\text{pulse}}$  = pulse duration

$z_r$  = distance, such that diagnosable portion of heated target remains

$c_s$  = sound speed



The heating pulse should be delivered in a time short compared to the time it takes for a rarefaction wave to reach an interior point, such that a significant portion of the target has reached maximum temperature.

# Basic Requirements

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**Temperature  $T > \sim 1$  eV to study Warm Dense Matter regime**

**Mass Density  $\rho \sim 0.01$  to 1.0 times solid density**

**Strong coupling constant  $\Gamma \sim 1$**

**For isochoric heating:  $\Delta t$  must be short enough to avoid cooling from hydrodynamic expansion**

**Uniformity:  $\Delta T/T < \sim 5\%$  (to distinguish various equations of state)**

**Low accelerator cost is a strong consideration, in present environment**

# A user facility for ion beam driven HEDP will have unique characteristics

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**Precise control** of energy deposition

**Uniformity** of energy deposition

**Large sample sizes** compared to diagnostic resolution volumes

Relatively **long times** allow equilibrium conditions

A **benign environment** for diagnostics

**High shot rates** (10/hour to 1/second) (simple targets and high accelerator rep rates)

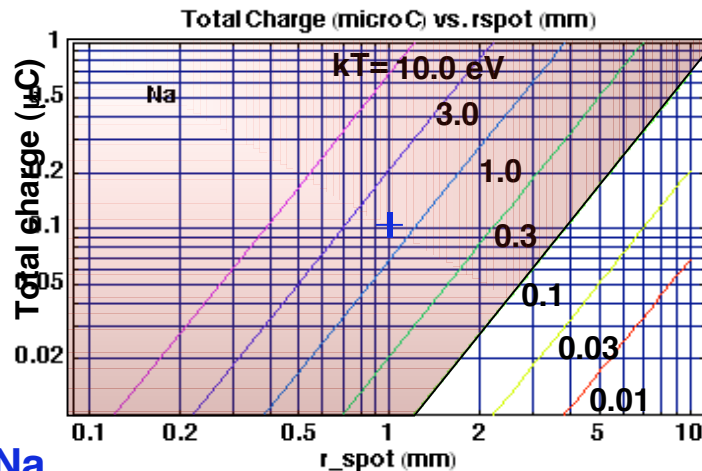


# Various ion masses and energies have been considered for Bragg-peak heating

Beam parameters needed to create a 10 eV plasma in 10% solid aluminum foam, for various ions  
(10 eV is equivalent to  $\sim 10^{11}$  J/m<sup>3</sup> in 10% solid aluminum)

Beam Ion	Z	A (amu)	Energy at Bragg Peak (MeV)	dE/dX at Bragg Peak (MeV-cm <sup>2</sup> /mg)	Foil Entrance Energy (app) (MeV)	Delta z for 5% T variation (10% solid Al) (microns)	Beam Energy for 10 eV (J/mm <sup>2</sup> )	t <sub>hydro</sub> = delta z/(2 cs) at 10 eV (ns)	Beam Power per sq. mm (GW/mm <sup>2</sup> )	Beam current for 1 mm diameter spot (A)
Li	3	6.94	1.6	2.68	2.4	22.1	3.3	0.5	6.1	1990.6
Na	11	22.99	15.9	11	23.9	53.5	8.0	1.3	6.1	200.3
K	19	39.10	45.6	18.6	68.4	90.8	13.6	2.2	6.1	69.8
Rb	37	85.47	158.0	39.1	237.0	149.7	22.4	3.7	6.1	20.2
Cs	55	132.91	304.0	59.2	456.0	190.2	28.5	4.7	6.1	10.5

# The parameters for a Neutralized Drift Compression Experiment (NDCX II) are chosen to heat target to reach WDM conditions



Na

$Z=11$ ;  $A=22.99$

$E_{\text{center of foil}} = 15.7 \text{ MeV}$

$E_{\text{foil entrance}} = 23.5 \text{ MeV}$  ( $\beta = 0.047$ )

$dE/dX = 10.13 \text{ MeV cm}^2/\text{mg}$

$Z = 5.75 \mu (\rho_{\text{al}}/\rho)$

$U = 8.7 \times 10^{10} \text{ J/m}^3 (1\text{mm}/r)^2 (q_{\text{tot}}/0.1\mu\text{C})(\rho/\rho_{\text{al}})$

$kT = 1.5 \text{ eV} (1\text{mm}/r)^2 (q_{\text{tot}}/0.1\mu\text{C})$

Without adiabatic lens:

$\Delta v/v_{\text{tilt}} = 0.05$

$\epsilon_N \leq 2.3 \text{ mm-mrad}$

$\delta p/p_{\text{rms}} = 0.2 \%$

(at 1 MV, 177 ns injector)

Target requirements set specifications for beam phase space at end of accelerator (and hence at injector)

- Longitudinal velocity spread limits pulse duration
- Emittance and chromatic aberrations limit spot radius
- Large velocity tilt allows shorter pulses but adds to chromatic aberration

Tradeoffs for compression factor of 20 and 1 mm final spot radius:

Velocity tilt (Head to tail) $dv/v_{\text{tilt}}$	Maximum rms velocity spread $dp/p_{\text{rms}}$ (before drift comp)	Maximum emittance unnormalized (mm-mrad)	Maximum normalized emittance (mm-mrad)	Beam radius at solenoid entrance $R_0$ (m)	Neutralized Drift length (m)	Maximum rms velocity spread $dp/p_{\text{rms}}$ (at injector)
0.05	7.22E-04	49.5	2.3	0.031	5.34	1.98E-03
0.1	1.44E-03	24.7	1.2	0.016	2.67	3.97E-03
0.2	2.89E-03	12.4	0.6	0.008	1.34	7.93E-03

# Parameters of experiments in the NDC sequence leading to a user facility (IBX/NDC)

	Existing machine, 1 year goal	3 - 5 year goal		10 year goal	
	NDCX-I	NDCX-II		NDCX-III (IBX-NDC)	
Ion Species	K <sup>+</sup>	Na <sup>+</sup>	Li <sup>+</sup>	Na <sup>+</sup>	Li <sup>+</sup>
Total Charge (μC)	0.002	0.1	0.3	0.3-1.0	1.0
Final Ion Energy (MV)	0.4	23.5	2.4	23.5	2.4
Final Pulse Duration (ns)	2	1	1	1	1
Final Spot Radius (mm)	0.5-1.0	1	1	1	1
Total pulse energy (J)	0.0008	2.4	0.72	7.1-24	2.4
Expected Target Temp (eV)	0.05 - 0.1	2 - 3	1 - 2	5-10	3

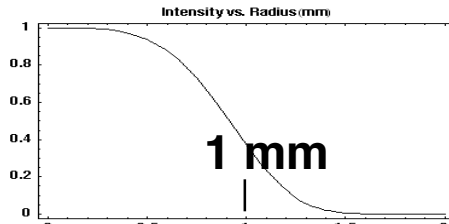
**NDCX = neutralized drift compression experiment**

**IBX = integrated beam experiment**

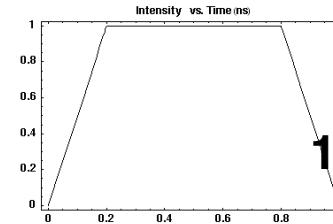
# We have begun using the 3D LLNL code HYDRA for our target studies

- A state-of-the-art multi-physics radiation transport/ hydrodynamics code by M. Marinak et al<sup>1</sup>
- Initial explorations of ion beam interactions with foil targets<sup>2</sup>:

Power vs.  
radius:

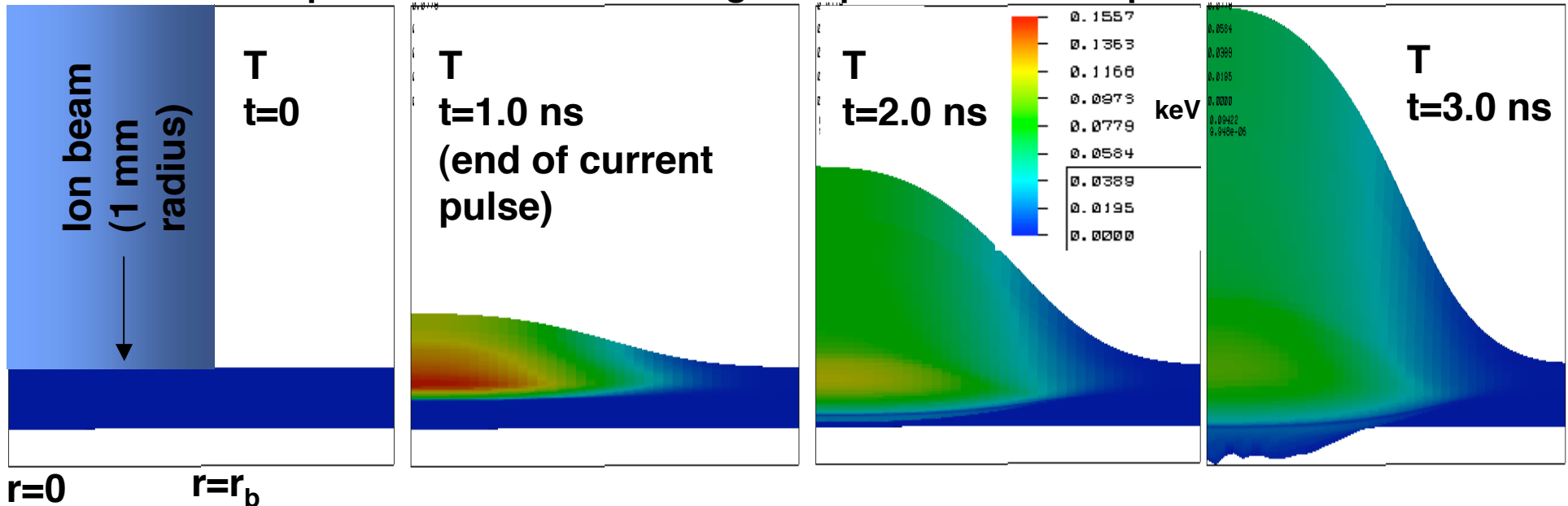


Power vs.  
time:



20 MeV Ne  
beam  
hitting 10% Al  
foam foil

Illustrative example of non-uniform heating: Temperature contour plot



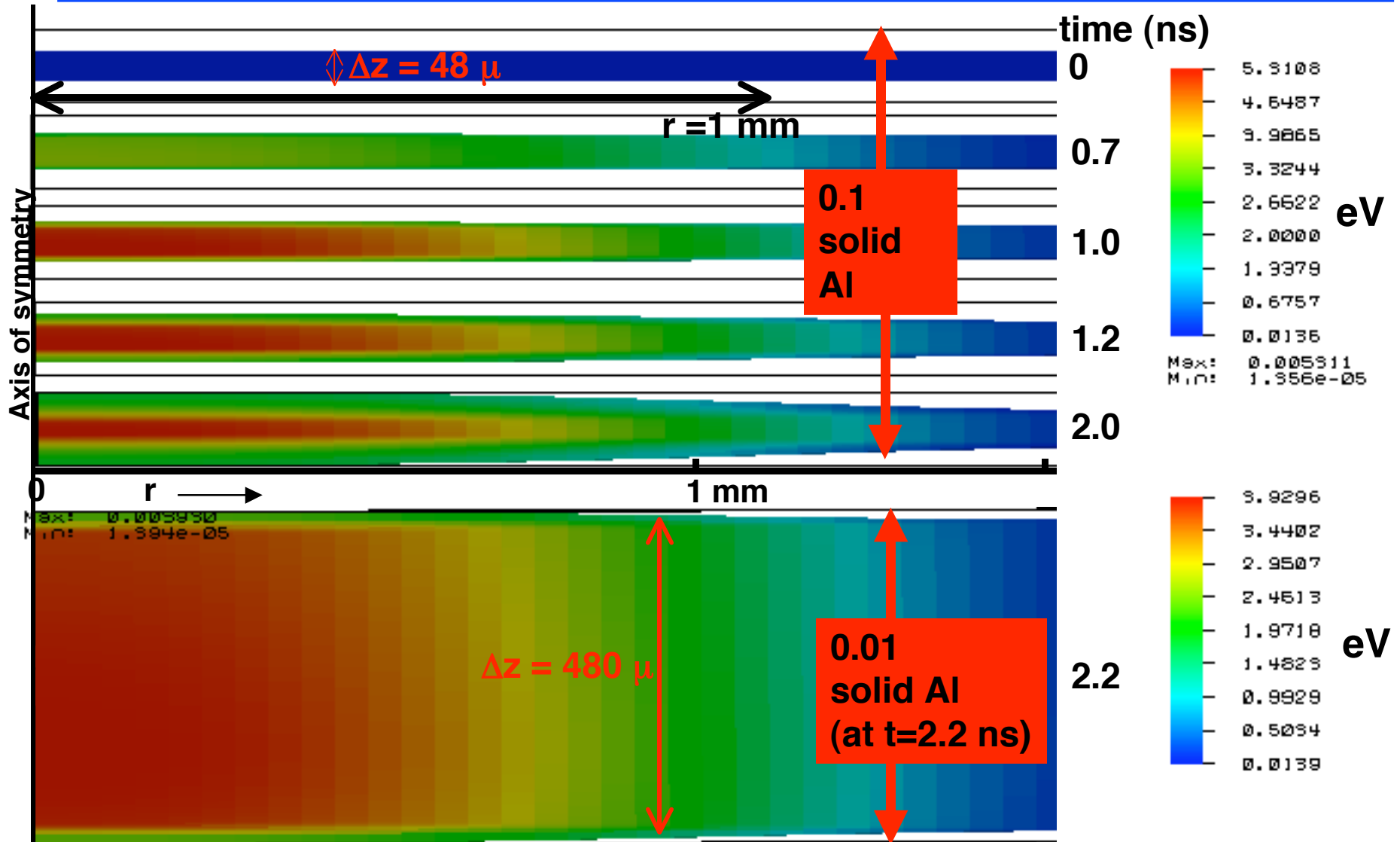
(2D [r-z], time-dependent simulations; Intensity 100 x higher, foil 3 x thicker for demo only)

1. M. M. Marinak, G. D. Kerbel, N. A. Gentile, O. Jones, D. Munro, S. Pollaine, T. R. Dittrich, and S. W. Haan, Phys. Plasmas 8, 2275 (2001).
2. Simulation collaborators: J.J. Barnard, G.E. Penn, J. S. Wurtele, P. Santhanam, A. Friedman, M. M. Marinak

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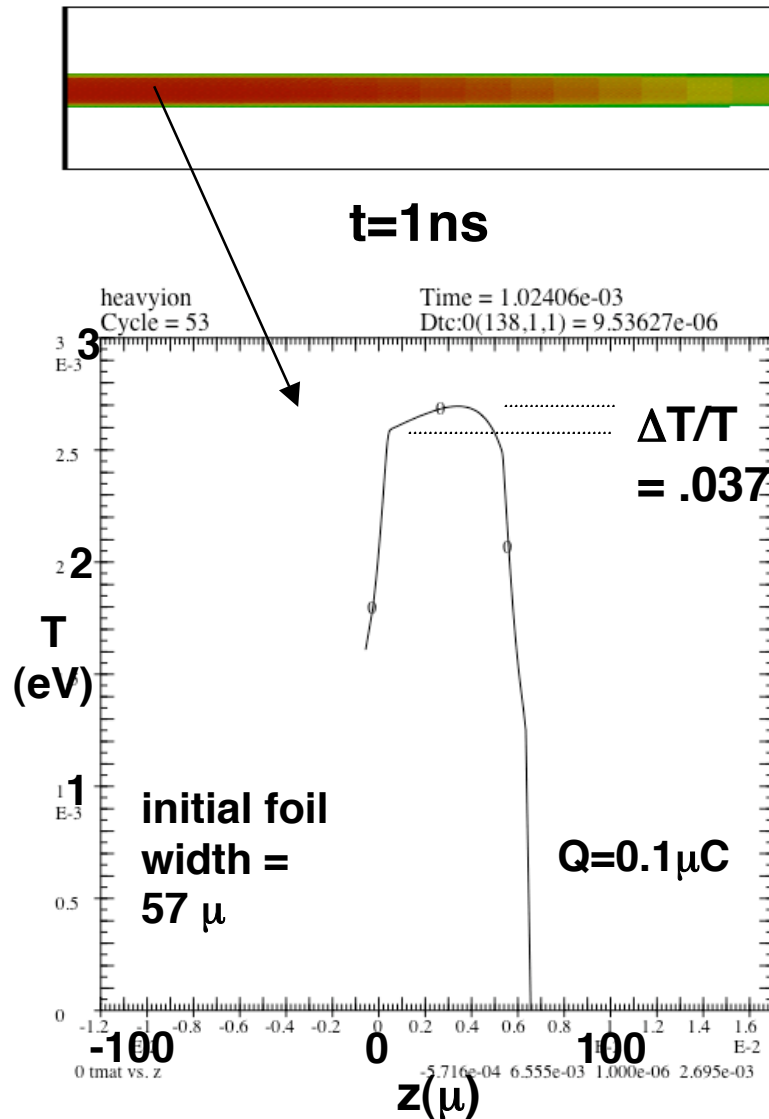


## Initial Hydra simulations confirm temperature uniformity of targets at 0.1 and 0.01 times solid density of Aluminum

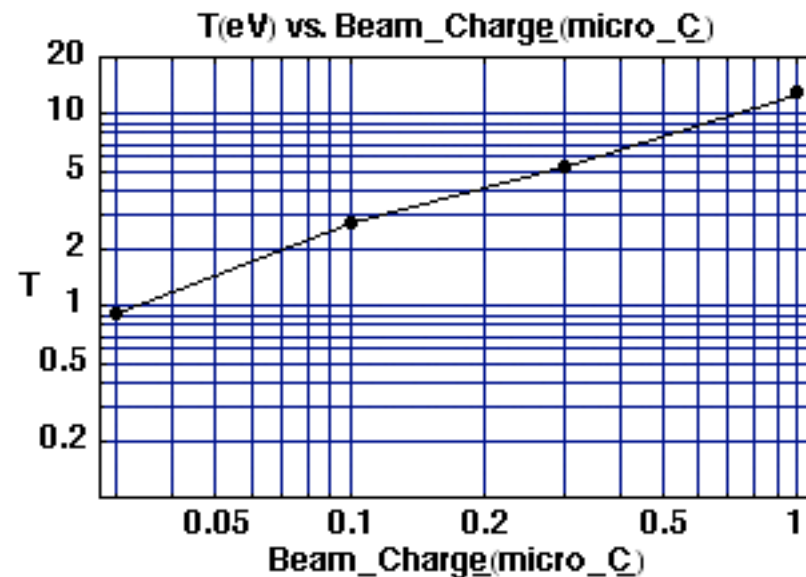


(simulations are for 0.3  $\mu\text{C}$ , 20 MeV Ne beam -- IBX/NDC parameters from workshop).

# For NDCX-II parameters, temperatures of a few eV could be achieved with high uniformity



## Variation of target temperature with total beam charge $Q$



(HYDRA results using QEOS, in Al 10% solid density; 23.5 MeV 1 mm Na<sup>+</sup> ion beam)

# New theoretical EOS work meshes well with experimental capabilities we will be creating

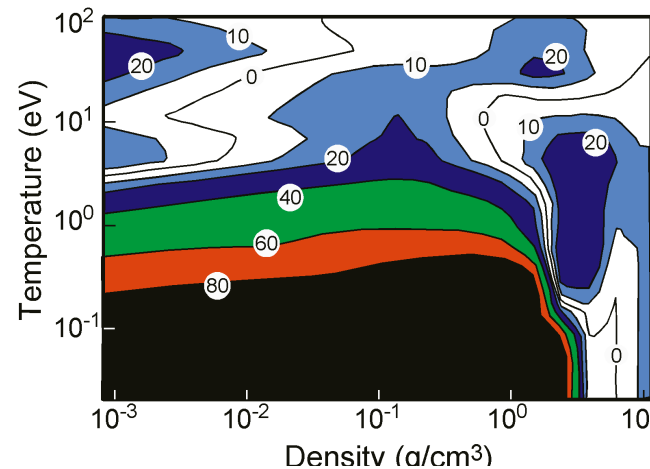
Large uncertainties in WDM region arise in the two phase (liquid-vapor) region

Getting two-phase regime correct will be main job for WDM

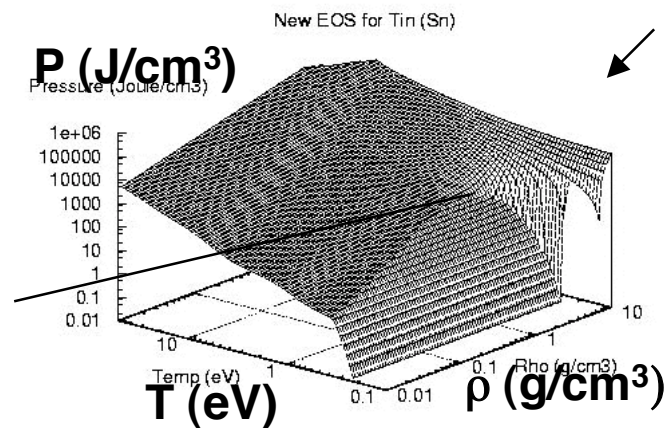
R. More has recently developed a new high quality EOS for Sn.

Interesting exactly in the  $\sim 1.0$  eV regime.

Critical point unknown for many metals, such as Sn



Plot of contours of fractional pressure difference for two common EOS (R. Lee)



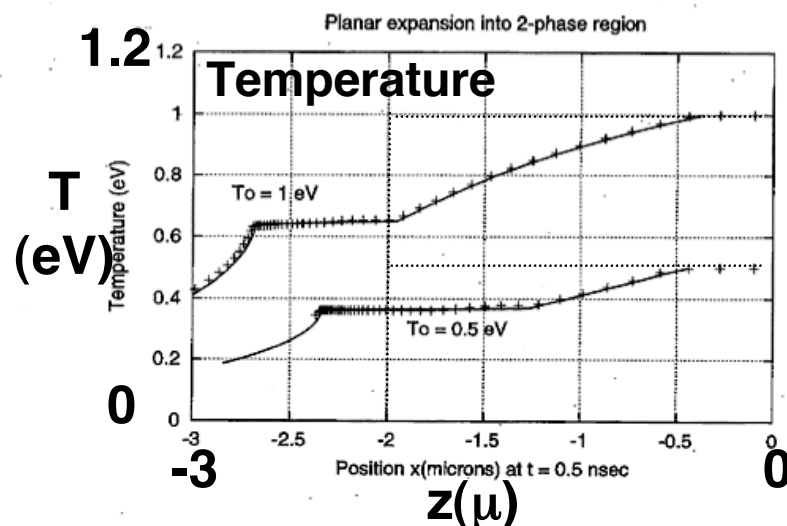
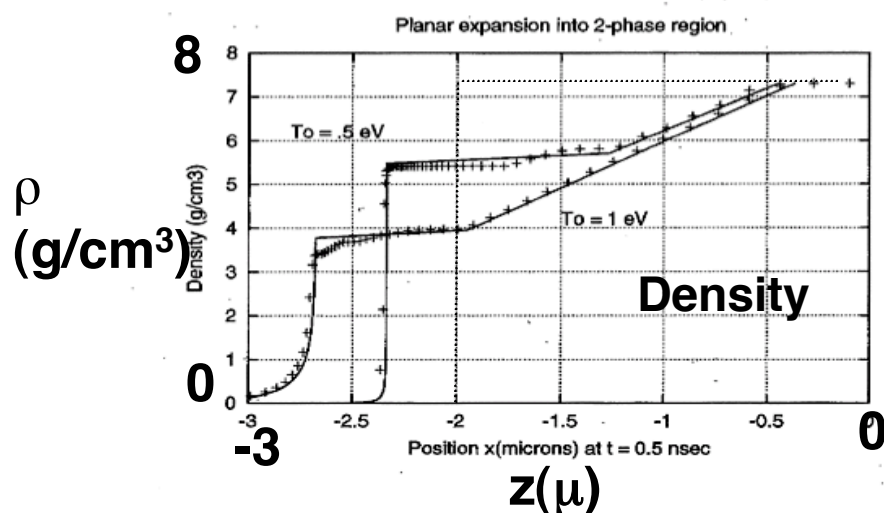
New EOS (cf R. More, T. Kato, H. Yoneda, 2005, preprint.)

EOS tools for this temperature and density range are just now being developed.

# New EOS predicts a sharp density cliff which may facilitate detection and help determine metallic critical points

R. More et al<sup>1</sup> have used a new EOS in 1D hydro calculations.  
EOS based on known energy levels and Saha equation (in contrast to QEOS, which uses “average” (Thomas Fermi) atom model)  
Two phase medium results in temperature and density plateaus with cliffs<sup>1,2</sup>

## Initial distribution



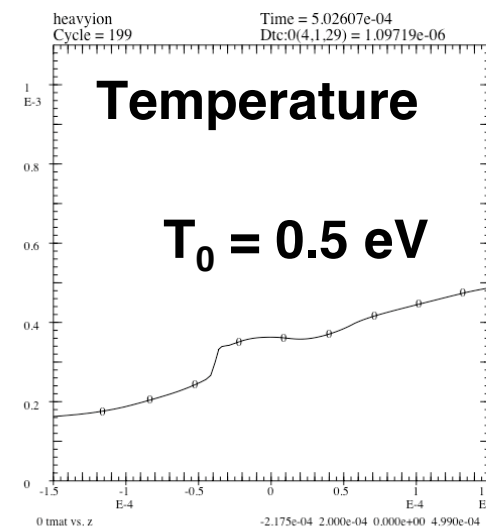
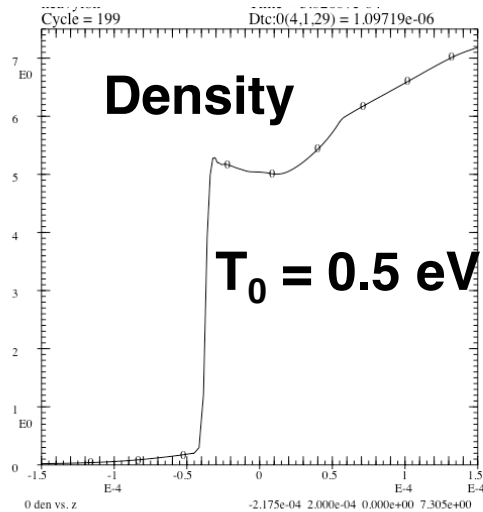
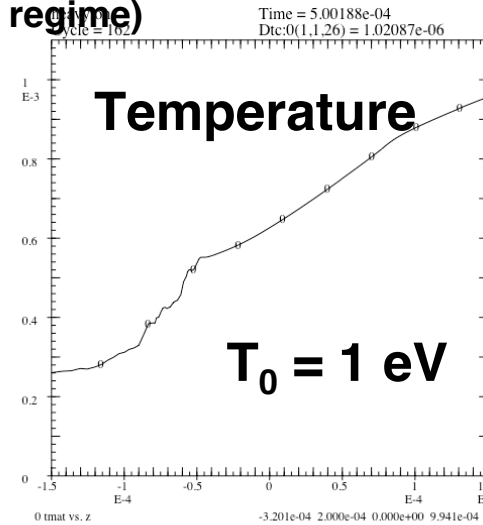
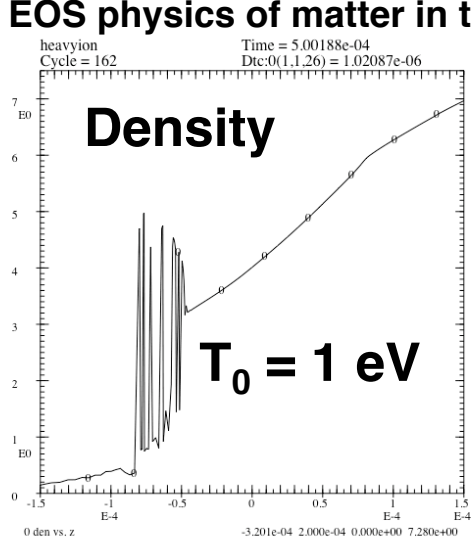
Example, shown here is initialized at  $T=0.5$  or  $1.0$  eV and shown at  $0.5$  ns after “heating.” Expect phenomena to persist for longer times and distances, but still to be explored.

<sup>1</sup>R. More, T. Kato, H. Yoneda, 2005, preprint. <sup>2</sup>Sokolowski-Tinten et al, PRL 81, 224 (1998)

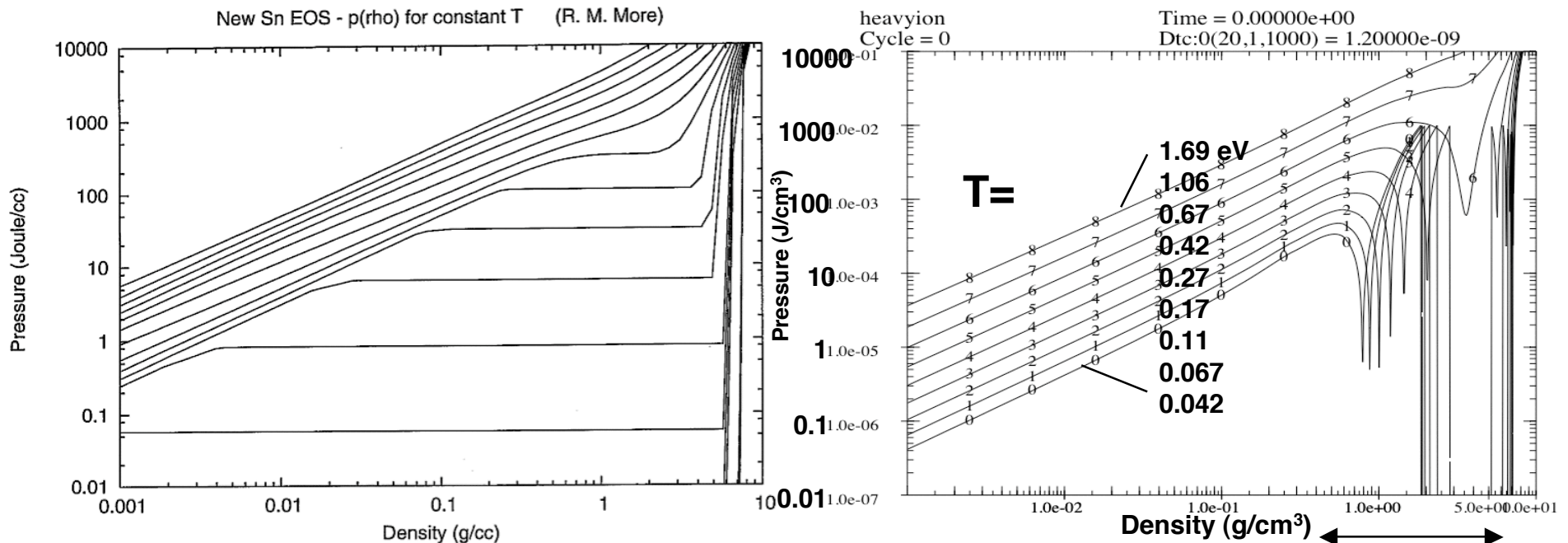


# HYDRA simulations show both similarities to and differences with R. More simulation of 0.5 and 1.0 eV Sn at 0.5 ns

(oscillations at phase transition at 1 eV may be due to numerical problems, but is more likely due to the different EOS physics of matter in the two-phase regime)



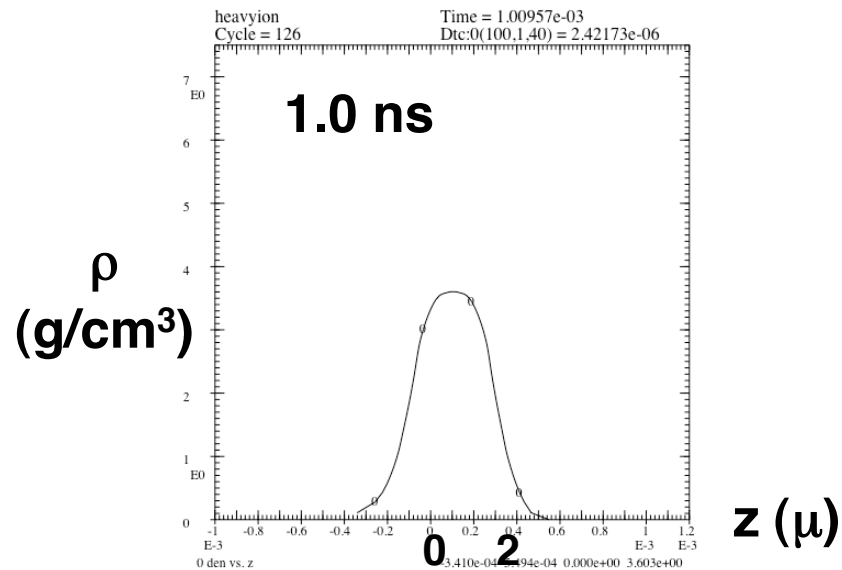
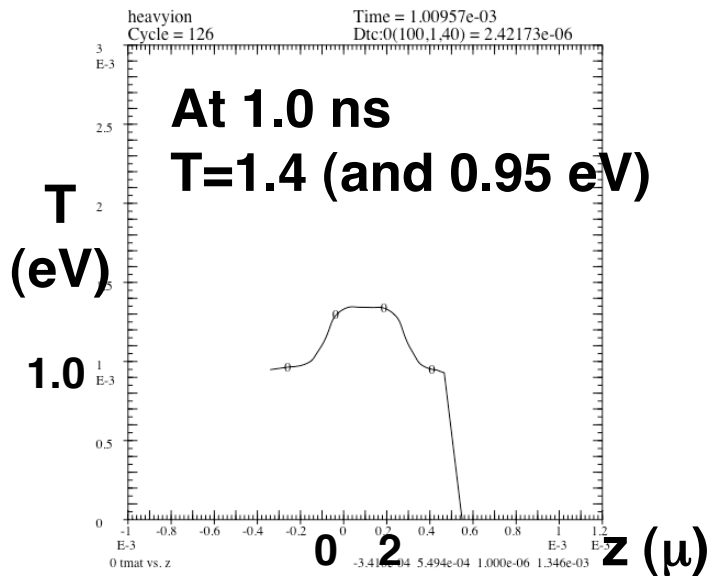
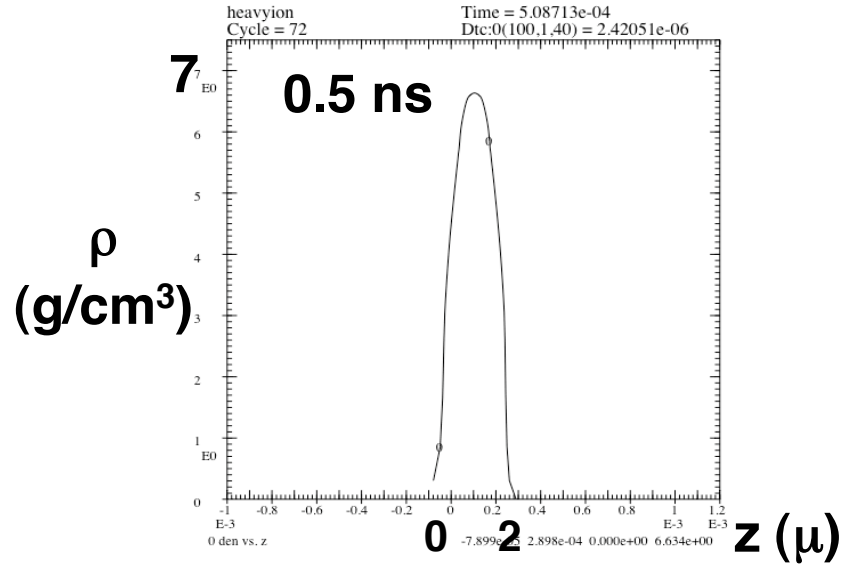
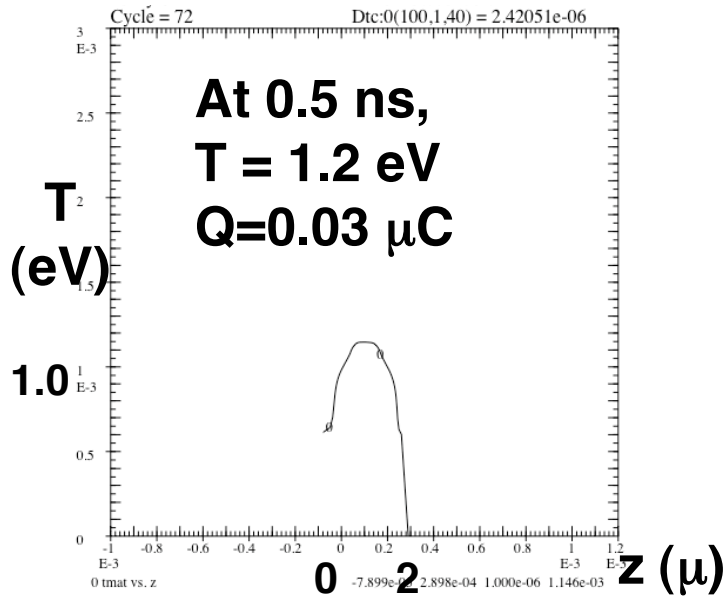
# Differences from HYDRA simulations and R. More simulations are likely due to differences in EOS



R. More EOS above includes two phase regime, whereby pressure is independent of average density, and material is a combination of liquid and vapor (i.e. bubbles) with microscopic densities at the extreme ends of the constant pressure segment, respectively

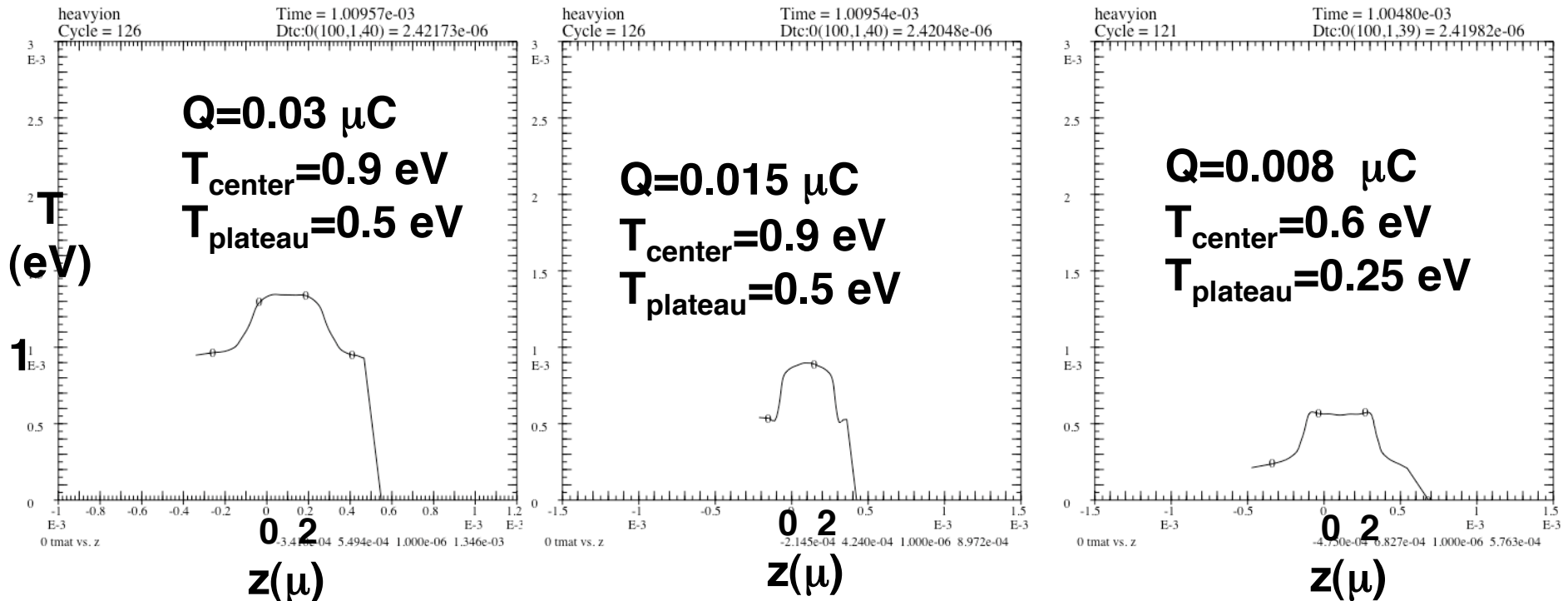
Hydra uses modified QEOS as one of its options. Decreasing  $\partial P / \partial \rho$  (at fixed T) indicated by arrow results in dynamically unstable material, so EOS becomes better modeled by a two-phase average pressure.

# Early explorations using Hydra of beam heating of Sn at solid density to ~1 eV shows evidence of T plateau



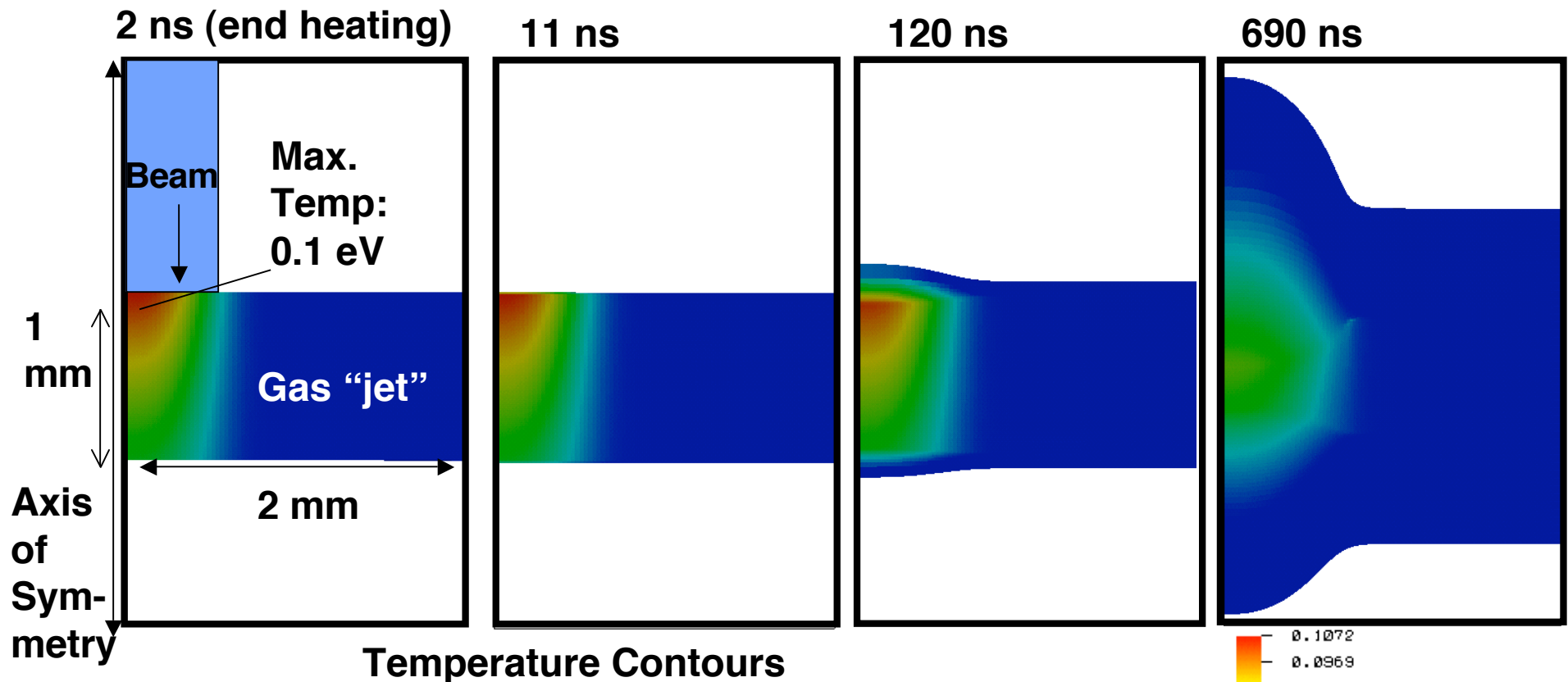
# Variation of temperature profiles for 2 $\mu$ Sn foil with various beam intensities, shows hints of predicted behavior

All plots are for 23.5 Na beam, after 1 ns



Existence of temperature plateaus appears related to passage of matter through 2-phase medium, but density plateaus not present, perhaps due to finite beam duration or differences in EOS

# We have used HYDRA to begin scoping possible near-term experiments on NDCX-I



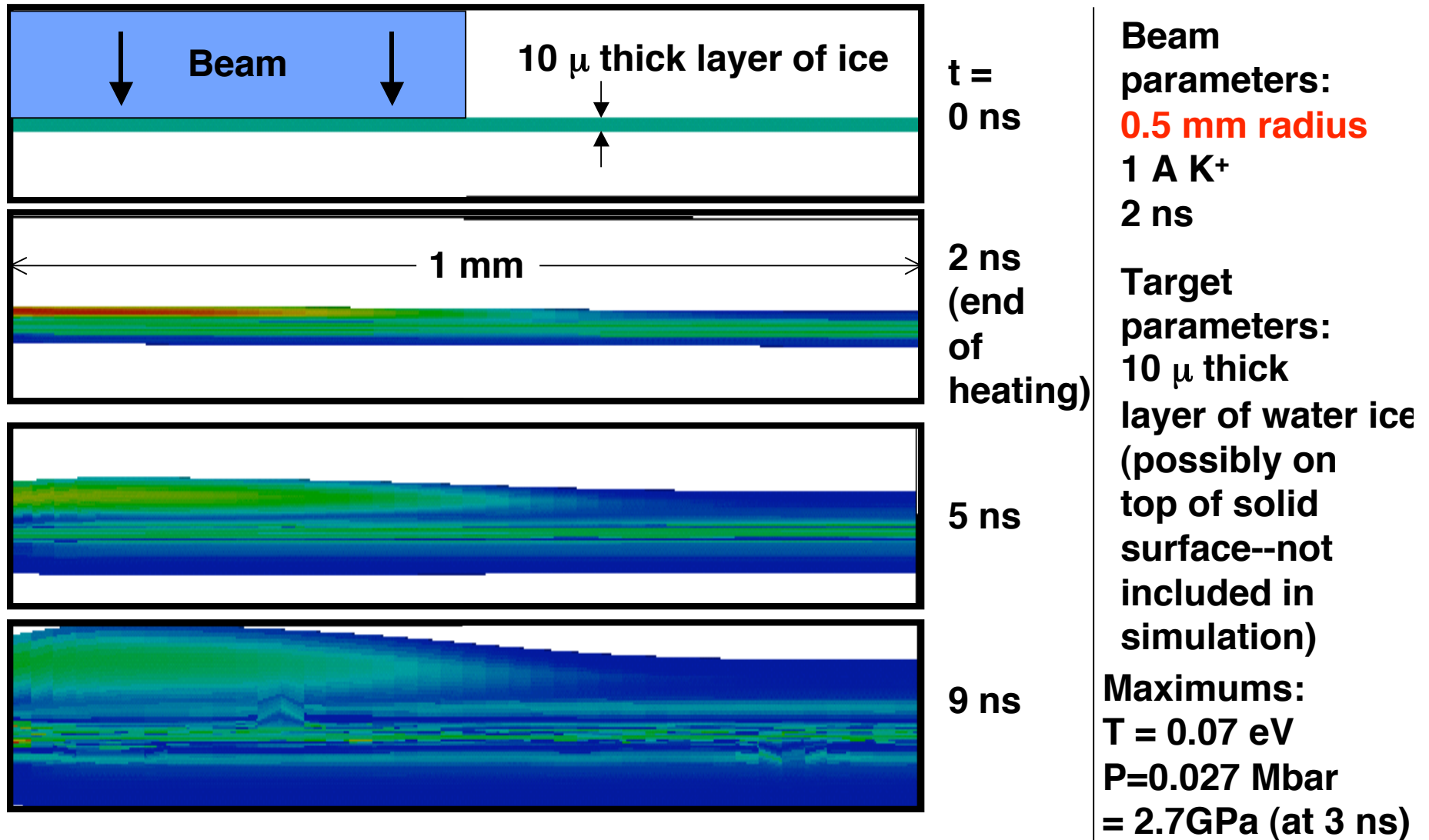
Simulation parameters:

Target: 1 mm thick Argon gas "jet" at 1 atmosphere

Beam: **0.5 mm radius**, 2 ns, 1A, K<sup>+</sup>

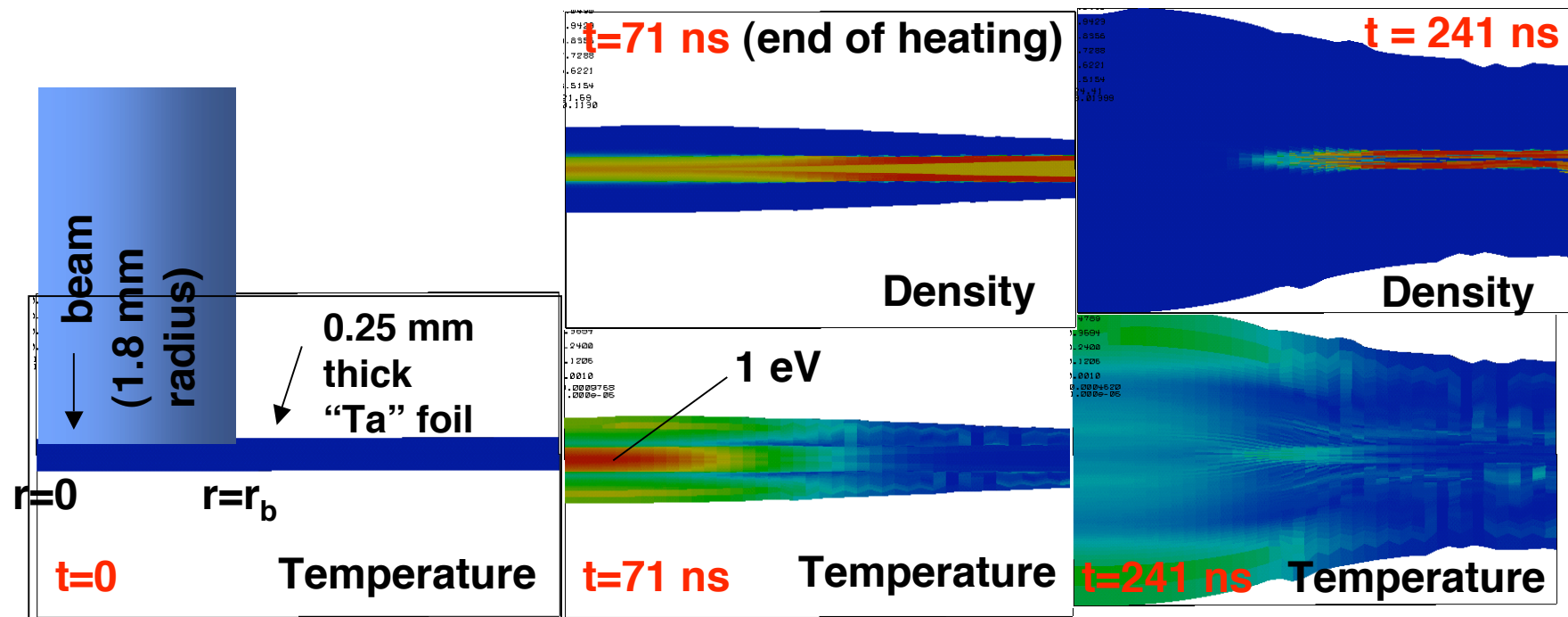
(final strong solenoid would be required for 0.5 mm spot)

Other near-term hydro experiments could be carried out with a frozen liquid (such as  $H_2O$ , iodine, mercury, etc.)

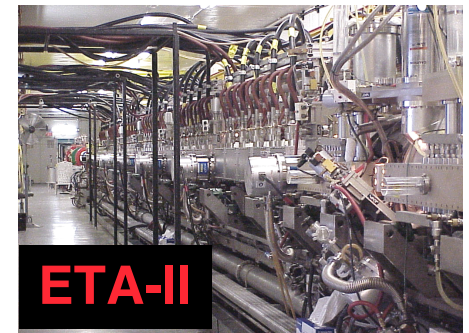


# Target experiments on ETA II, could also provide target experience in interesting regime

Example: “Tantalum-like” foil, with equivalent 40 GeV proton beam

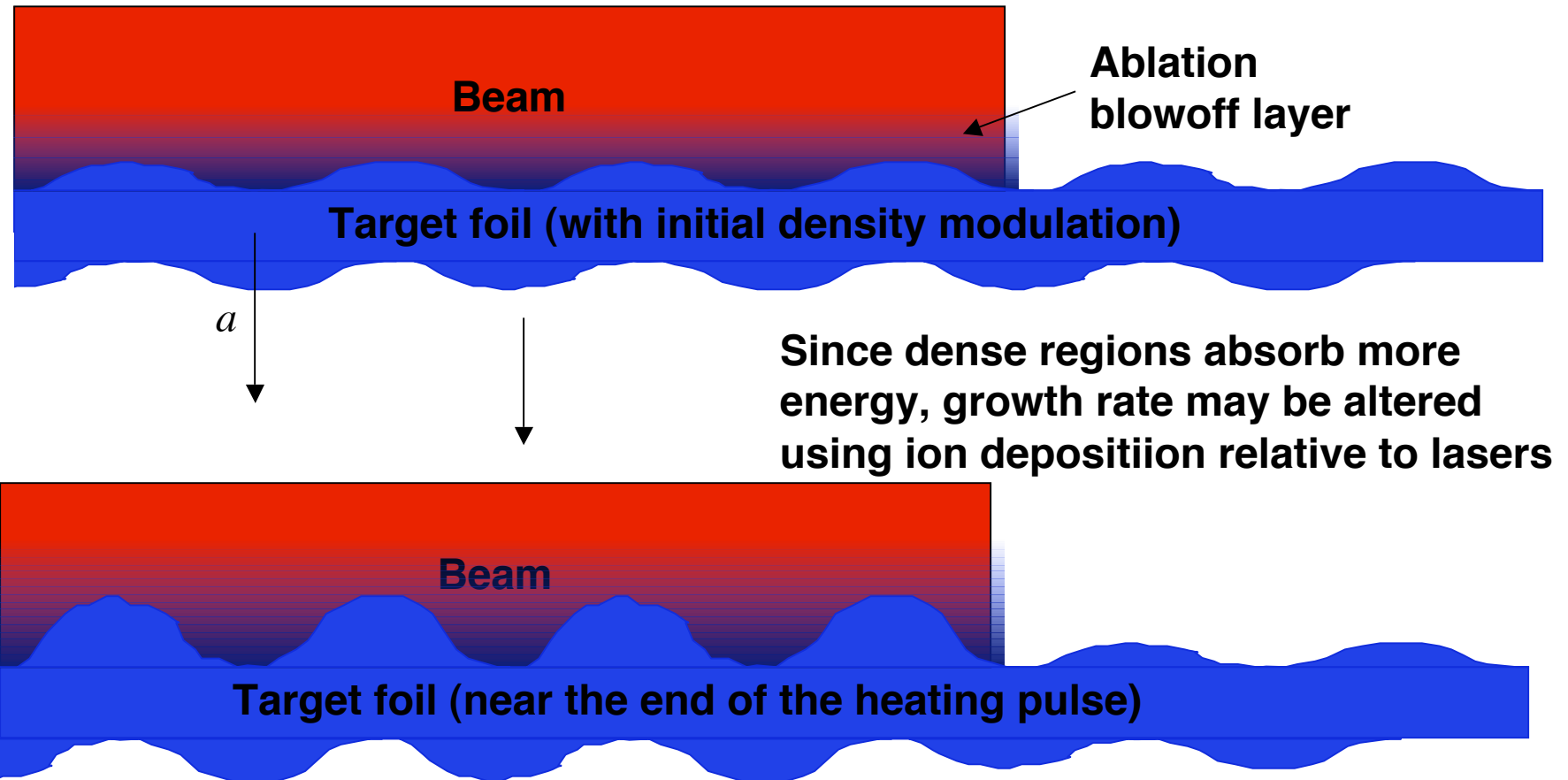


- ETA II parameters: 5 MeV e-, 2 kA, 50 ns,
- Need to adapt electron beam deposition to include scattering





## Energy deposition using ion beams may alter the growth rate of the Rayleigh-Taylor instability relative to lasers



Growth rate  $\gamma$  (for laser deposition) :  $\gamma \approx (k a / (1 + k L))^{1/2} - \alpha k V_a$ , where  $k$  is the wave number of the perturbation,  $a$  is the acceleration rate,  $L$  is the density-gradient scale length,  $\alpha$  is a constant between 1 and 3,  $V_a$  is the velocity of the ablation front (Lindl, 1998<sup>1</sup>)

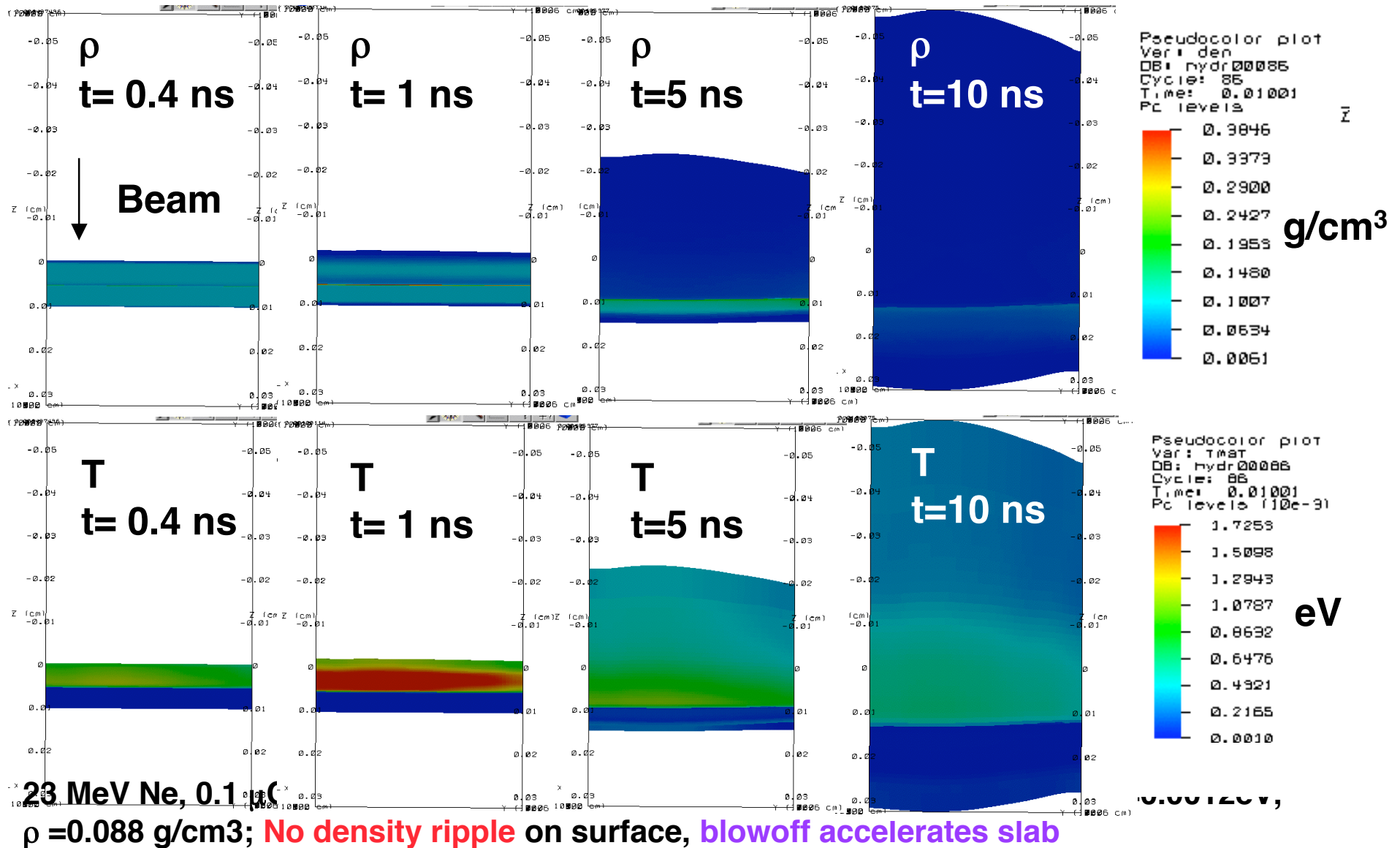
1. John D. Lindl, "Inertial Confinement Fusion," Springer-Verlag, NY, 1998

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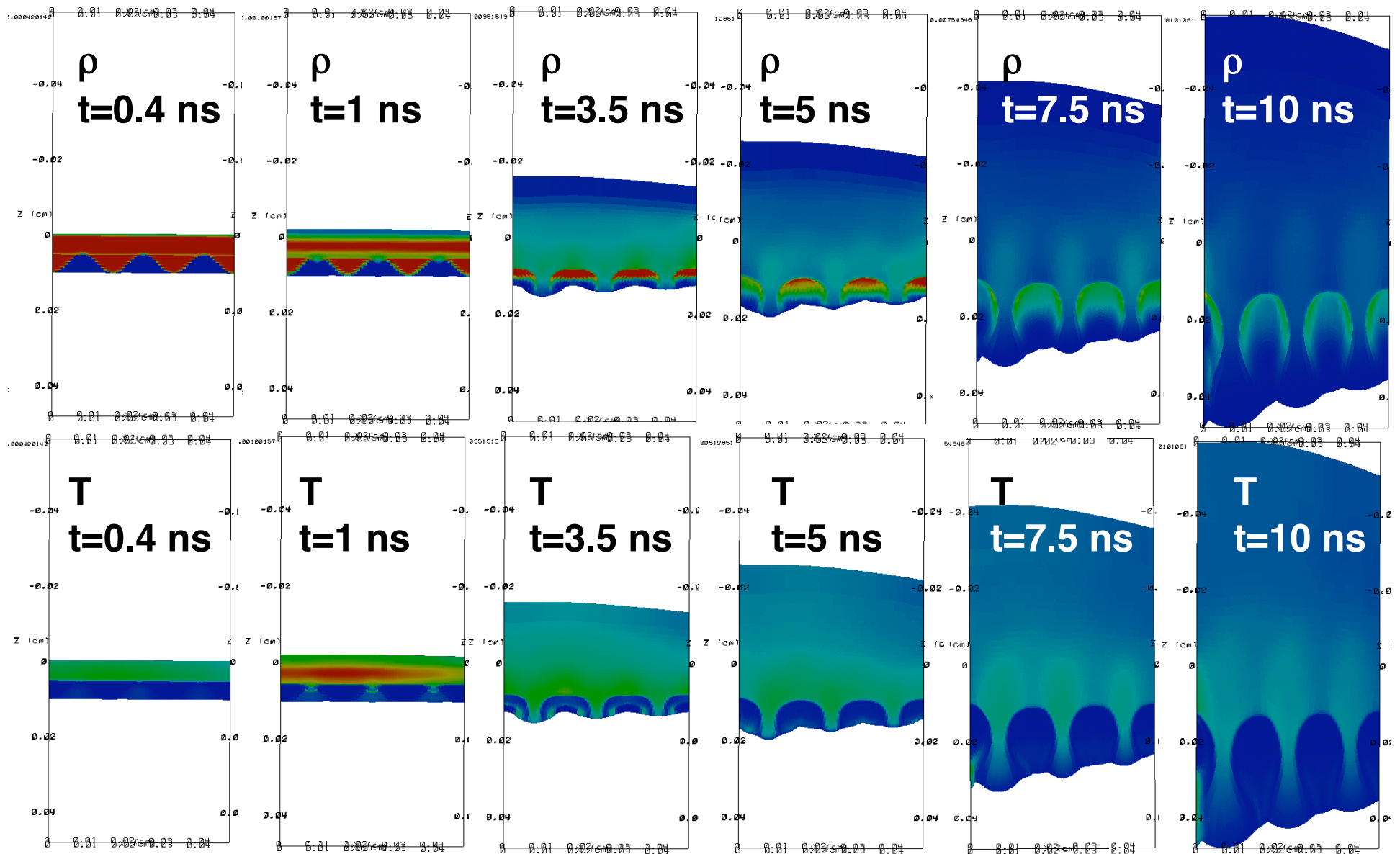




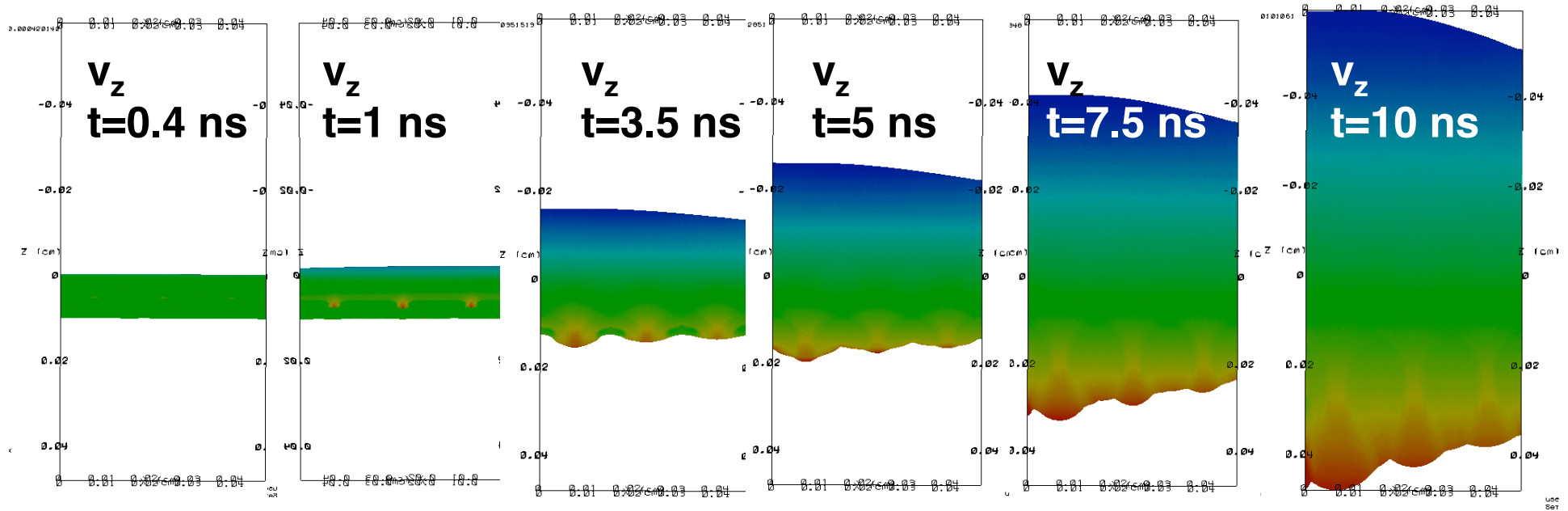
# We have begun using Hydra to explore accelerator requirements to study beam driven Rayleigh Taylor instability



# When **initial surface ripple** is applied, evidence for Rayleigh Taylor instability is suggestive

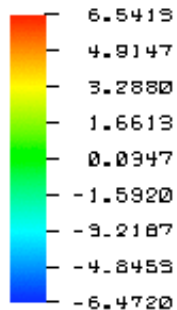


# When initial surface ripple is applied, evidence for Rayleigh Taylor instability is suggestive (-- continued)



Scale  
for above  
figures  
( $v_z$ ):

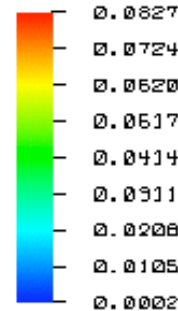
Pseudocolor plot  
Var: zdot  
DB: hydr02678  
Cycle: 2678  
Time: 0.005207  
Pc levels



cm/ $\mu$ s

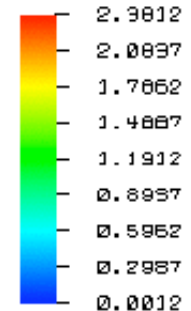
Scales  
from  
previous  
page  
( $\rho$  and T)

Pseudocolor plot  
Var: den  
DB: hydr02812  
Cycle: 2812  
Time: 0.007543  
Pc levels



g/cm<sup>3</sup>

Pseudocolor plot  
Var: tmet  
DB: hydr00023  
Cycle: 23  
Time: 0.0005232  
Pc levels (10e-5)



eV

## **We have begun establishing target requirements for WDM studies and translating to requirements on the accelerator**

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**We are quantitatively exploring the tradeoffs involved in focusing the beam in both space and time**

**We are using a state-of-the-art rad-hydro(HYDRA) simulation code to evaluate targets for WDM study. We are also comparing HYDRA with lower-dimensional codes, but using advanced EOS models**

**Several potential experiments are being considered including:**

- EOS/conductivity experiments on ETA-II**
- NDCX-I experiments heating condensed ices**
- Two-phase experiments on NDCX-II, IBX/NDC**
- Rayleigh-Taylor experiments on NDCX-II, IBX/NDC**

**Future simulations and calculations will simulate in detail many of these potential experiments**

# EXTRAS

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